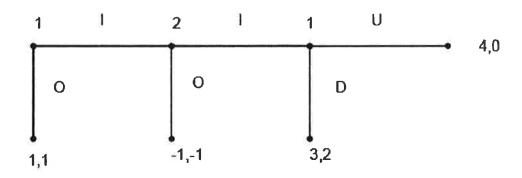


## YLIOPISTOTENTTI - UNIVERSITY EXAM

Opiskelijan nimi / Student name:			Opiskelijanumero / Student number:	
Opettaja täyttää / Lecturer fi	lls in:			
Opintojakson koodi and nim	i / The code and the nam	e of t	ne course:	
Koodi / Code 721342	S			
Tentin nimi / Exam n	ame Game Theory			
Tiedekunta / Faculty:				
Tentin pvm / Date of exam: 18.9.2017		Tenti	entin kesto tunteina / Exam in hours: 3	
Tentin nro / No. of the exam: 2. uusinta (esim. Tentti, 1. uusinta, 2. uusinta / e.g. Exam, 1. retake, 2. retake)		Opin	topistemäärä / Credit units: 6	
Tentaattori(t) / Examiner(s): Marja-Liisa Halko		Sisäinen postios. / Internal address:		
Politiikan ja talouden tutkimuksen laitos		PL 17, 00014 Helsingin yliopisto		
Sallitut apuvälineet / The de	vices allowed in the exar	n:		
☑ Nelilaskin /	⊠ Funktiolaskin /		$\square$ Ohjelmoitava laskin /	
Standard calculator	Scientific calculator		Programmable calculator	
🗌 🗆 Muu materiaali, tarkenne	ttu alla / Other material, s	pecifie	ed below:	
			a	
Tenttiin vastaaminen / Pleas				
│ ⊠ Suomeksi / in Finnish	🛭 Englanniksi / in E	nglish		
	· ·	-	n oikeus käyttää arvioitavassa	
opintosuorituksessa suomen vieraan kielen opintoja. (Kts.			uskieli olisi englanti. Tämä ei koske	
			innish language for their study	
attainment, even though the	language of instruction is	Englis	h, (excluding language studies) even the Education Regulations 18 §)	
Kysymyspaperi on palautett ⊠ Kyllä / Yes	ava / Paper with exam qu	estion	ns must be returned:	

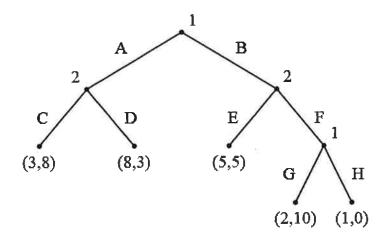
Answer all the questions (1-5). NOTE! As you will answer the question 5 in this question paper, please return this paper with your answers.

- 1. Each of two political parties can choose to buy time on commercial radio shows to broadcast negative ad campaigns against its rival. These choices are made simultaneously. Government regulations forbid a party from buying more than 2 hours of negative campaign time, so that each party cannot choose an amount of negative campaigning above 2 hours. Given a pair of choices  $(a_1, a_2)$ , the payoff of party 1 is  $v_1(a_1, a_2) = a_1 2a_2 + a_1a_2 (a_1)^2$  and the payoff of party 2 is  $v_2(a_1, a_2) = a_2 2a_1 + a_1a_2 (a_2)^2$ .
- (a) What is the best-response function for each party? (2 points)
- (b) What is the pure-strategy Nash equilibrium? (3 points)
- 2. Consider the following extensive form game:



- (a) Write the game in normal form and solve its Nash equilibria. (3 points)
- (b) Solve the subgame perfect equilibria of the game. Does the game have Nash equilibria that are not subgame perfect equilibria? (3 points)

3. Write the game below in normal form and solve its Nash equilibria (in pure strategies). (5 points)



4. Show first that in the game below, the player 2 has a mixed strategy that dominates her strategy L (3 points). Remember then that a rational player does not play dominated strategies and solve all (pure and mixed) Nash equilibria of the game. (6 points)

			P2	
		L	M	R
P1	Т	2,2	0,3	1,2
	В	3,1	1,0	0,2

5. Consider the following Battle of sexes -game between a husband and a wife:

## (a) Loving

		Wife	
		F	Ο
Husband	F	3,1	0,0
	Ο	0,0	1,3

## (b) Leaving

		Wife	
		F	Ο
Husband	F	3,0	0,1
	Ο	0,3	1,0

The husband prefers F to O, but would rather be together than apart. The husband is not sure of his wife's preferences. He does not know if his wife likes to be with him (loving) or if she prefers to go either event by herself (leaving). The wife knows her own preferences. The husband believes that with probability  $\rho$  the wife is loving and with probability  $1 - \rho$  she is leaving. The wife knows the beliefs of the husband (knows  $\rho$ , common prior).

- a) First draw the game in an extensive form, where an artificial player, "nature", first selects the type of the wife. Remember to be careful with the information sets. (4 points)
- b) Does any player (or any player type) have a dominant strategy? Explain. (4 points)

statements are	true of false. For every correct answer you will get two (2) points and for every wrong
answer you w	ill get minus one point (-1). If you do not answer anything, you will get zero points.
Note! Howeve	er, the lower limit of your points is zero points. (max 12 points)
Write next the	Bayesian normal form of the game. Let's first write the strategies of the players.
STATEMEN	$\Gamma$ 1: Husband has four strategies, because he does not know, whether his wife is loving or
leaving.	
☐ True	□ False
STATEMEN'	$\Gamma$ 2: Wife has four strategies, because she knows whether she is loving or leaving.
☐ True	☐ False
□ True	□ 1.×arse
STATEMEN	$\Gamma$ 3: Husband's payoffs depend on the probability $ ho$ because he does not know, whether his
wife is loving o	r leaving, but the wife's payoffs do not depend on the probability $ ho$ .
☐ True	☐ False
	$\Gamma$ 4: If both players always choose F, the payoff of the husband is 3 and the payoff of the
wife is $\rho$ .	
☐ True	□ False
Next we use the	e Bayesian normal form to solve the Nash equilibria of the game (or bayesian Nash equilibria).
	um, neither of the players wants to deviate from the equilibrium strategy and choose some
other strategy.	
	1
STATEMEN'	$\Gamma$ 5: If $\rho < \frac{1}{4}$ , then the game does not have a Nash equilibrium.
☐ True	□ False
STATEMEN!	$\Gamma$ 6: If $\rho \geq \frac{1}{4}$ , there exists an equilibrium where both husband and wife always choose F.
	7
☐ True	☐ False

(c) In the following, there are six statements relating to the solution of the problem. Indicate whether these

