



## YLIOPISTOTENTTILOMAKEPOHJA / UNIVERSITY EXAM TEMPLATE

Koskee tiedekuntia LuTK, OyKKK, KaTK, TTK, TST ja BMTK (Linnanmaan tentit) /  
Concerns Faculties SCI, OBS, OMS, TECH, ITEE and BMM (Linnanmaa campus)

<b>Tentin päivämäärä / Date of exam:</b> 20.01.2016	<b>Tentin kesto tunteina / Exam in hours: 4h</b>
<b>Tiedekunta / Faculty: Oulun yliopiston kauppakorkeakoulu / Oulu Business School</b>	
<b>Opintojakson koodi, nimi ja tentin numero / The code and the name of the course and number of the exam: 721345S, Intermediate Microeconomics, 2nd Retake Exam</b>	
<b>Tentaattori(t) / Examiner(s): Enni Ruokamo, Hannu Huuki</b>	<b>Sisäinen postios. / Internal address</b> 60yKKK
<b>Sallitut apuvälineet / The devices allowed in the exam:</b>	
<input checked="" type="checkbox"/> Nelilaskin / Standard calculator	<input checked="" type="checkbox"/> Funktiolaskin / Scientific calculator
<input type="checkbox"/> Ohjelmoitava laskin / Programmable calculator	
<input type="checkbox"/> Muu materiaali, tarkennettu alla / Other material, specified below:	
<b>Tenttiin vastaaminen / Please answer the questions:</b>	
<input checked="" type="checkbox"/> Suomeksi / in Finnish	<input checked="" type="checkbox"/> Englanniksi / in English
<b>Kysymyspaperi on palautettava / Paper with exam questions must be returned:</b>	
<input checked="" type="checkbox"/> Kyllä / Yes	<input type="checkbox"/> Ei / No

*Answer to all 5 questions.*

1.

Consider the following statements if they are true or false. Verify your answers briefly. In order to get the credit from the correct answer the explanation is needed.

- a) Indifference curves can never intersect with each other. 1p
- b) For goods  $x_1$  and  $x_2$  the marginal rate of substitution describes the market price ratio  $p_1/p_2$ . 1p
- c) A Giffen good is a good that decreases in demand as income decreases. 1p
- d) A bond paying 1000€ each year forever with an annual discount rate of 6% has a present value of 6000€. 1p
- e) If firm has a production function of the form  $y = f(x_1, x_2) = x_1^{0.3}x_2^{0.7}$ , where  $x_i$  is the amount of input  $i$  and  $y$  is the amount of output, it exhibits constant returns to scale. 1p
- f) Adverse selection refers to situation where one side of the market can't observe the actions of the other side. 1p

2.

Intertemporal choice, two period model:

Consumer has preferences:  $U(c_1, c_2) = c_1c_2$ ,

where  $c_1$  is consumption in period 1 and  $c_2$  is consumption in period 2.

Let  $m_1$  and  $m_2$  be the incomes received in periods 1 and 2.

The interest rate is  $r$ .

Ignore the price effects by setting the prices in periods 1 and 2 to one:  $p_1 = p_2 = 1$ .

- a) Write down the intertemporal budget constraint? 2p
- b) Consumer maximizes intertemporal utility.  
Solve the optimized consumption levels  $c_1^*(m_1, m_2, r)$  and  $c_2^*(m_1, m_2, r)$ . 3p
- c) Set  $m_1 = 10, m_2 = 21$  and  $r = 5\%$ .  
Is the consumer a saver or a borrower? 1p

3.

Danny has a utility function of the form  $u(w) = \sqrt{w}$ . He initially has wealth  $w$  of 4€. He has a lottery ticket that will be worth 12€ with probability  $1/2$  and will be worth 0€ with probability  $1/2$ .

- a) What are Danny's preferences towards risk. Is he risk loving, risk averse or risk neutral? Explain your answer by studying the shape of the utility function analytically and/or graphically. 3p
- b) What is Danny's expected utility of participating into this lottery? 2p
- c) What is the lowest price  $p$  at which he would sell his lottery ticket? 1p

4.

- a) Explain the concept of (own) price elasticity of demand. Calculate the elasticity of demand for a linear demand  $D(p) = a - bp$ , where  $a$  and  $b$  are parameters,  $p$  is price and  $D(p)$  is quantity demanded. 2p
- b) What marginal product measures? Calculate the marginal products of capital (K) and labor (L), when the production function is  $y = f(K, L) = \sqrt{K} + (1/3)L$ . Is the marginal product of capital  $MP_K$  diminishing, increasing or constant? Is the marginal product of labor  $MP_L$  diminishing, increasing or constant? 2p
- c) What is meant by technical rate of substitution (TRS)? Suppose the firm's production function is  $y = f(K, L) = K^{1/3}L^{2/3}$ . Calculate the TRS at a point, where the firm employs 4 units of capital (K) and 8 units of labor (L). 2p

5.

In a small town there are two bakers, A and B, baking identical breads  $b_A$  and  $b_B$ .  
The cost function for both bakers is  $c(b) = 4b$ .  
The inverse market demand curve for bread is  $p(b) = 100 - 2b$ .

First, study the market with Cournot duopoly model, where each firm chooses its output to maximize its profits given the output that it expects the other firm to produce.

- a) Calculate the reaction functions  $R_A(b_B)$  and  $R_B(b_A)$ . Draw a graph illustrating these functions, where output  $b_A$  is on the horizontal axis and output  $b_B$  is on the vertical axis. Solve the Cournot-Nash equilibrium  $(b_A^*, b_B^*)$ , and point it on your graph. How much will baker A produce? How much will baker B produce? What is baker A's profit? What is baker B's profit.  
3p

Now, suppose the producers operate in a Stackelberg-market model. Baker A begins early, and acts as a Stackelberg-leader. Baker B is a Stackelberg-follower.

- b) Write down baker A's profit maximization problem.  
Solve leader's Stackelberg output  $b_A^S$ .  
Solve follower's Stackelberg output  $b_B^S$ .  
2p

Finally, suppose the producers operate in a Bertrand-market model. Both bakers set their prices simultaneously.

- c) What is the Nash equilibrium price  $p^*$  in this framework?  
Explain the adjustment process of price setting.  
1p